

## 2.1

$S \rightarrow (L) \mid a$

$L \rightarrow L-S \mid S$

(1)  $S \rightarrow (L)$

(2)  $S \rightarrow a$

(3)  $L \rightarrow SL'$

(4)  $L' \rightarrow -SL'$

(5)  $L' \rightarrow \epsilon$

	<i>FIRST</i>	<i>FOLLOW</i>
S	(, a	\$, -, )
L	(, a	)
L'	-, ε	)

	<i>a</i>	<i>(</i>	<i>)</i>	<i>-</i>	<i>\$</i>
<i>S</i>	$S \rightarrow a$ (2)	$S \rightarrow (L)$ (1)			
<i>L</i>	$L \rightarrow SL'$ (3)	$L \rightarrow SL'$ (3)			
<i>L'</i>			$L' \rightarrow \epsilon$ (5)	$L' \rightarrow -SL'$ (4)	

#S	(a-a-a)\$	ε
#)L(	(a-a-a)\$	1
#)L	a-a-a)\$	1
#)L'S	a-a-a)\$	13
#)L'a	a-a-a)\$	132
#)L'	-a-a)\$	132
#)L'S-	-a-a)\$	1324
#)L'S	a-a)\$	1324
#)L'a	a-a)\$	13242

#)L'	-a)\$	13242
#)L'S-	-a)\$	132424
#)L'S	a)\$	132424
#)L'a	a)\$	1324242
#)L'	)\$	1324242
#)	)\$	13242425
#	\$	13242425

## 2.2

$S \rightarrow (L) \mid a$

$L \rightarrow S-L \mid S$

- (1)  $S \rightarrow a$
- (2)  $S \rightarrow (L)$
- (3)  $L \rightarrow SL'$
- (4)  $L' \rightarrow -L$
- (5)  $L' \rightarrow \epsilon$

	<i>FIRST</i>	<i>FOLLOW</i>
S	a, (	\$, -, )
L	a, (	)
L'	-, $\epsilon$	)

	<i>a</i>	<i>(</i>	<i>)</i>	<i>-</i>	<i>\$</i>
<i>S</i>	$S \rightarrow a$ (1)	$S \rightarrow (L)$ (2)			
<i>L</i>	$L \rightarrow SL'$ (3)	$L \rightarrow SL'$ (3)			
<i>L'</i>			$L' \rightarrow \epsilon$ (5)	$L' \rightarrow -L$ (4)	

#S	((a)-a)\$	$\epsilon$
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#)L(	((a)-a)\$	2
#)L	(a)-a)\$	2
#)L'S	(a)-a)\$	23
#)L')L(	(a)-a)\$	232
#)L')L	a)-a)\$	232
#)L')L'S	a)-a)\$	2323
#)L')L'a	a)-a)\$	23231
#)L')L'	)-a)\$	23231
#)L')	)-a)\$	232315
#)L'	-a)\$	232315
#)L-	-a)\$	2323154
#)L	a)\$	2323154
#)L'S	a)\$	23231543
#)L'a	a)\$	232315431
#)L'	)\$	232315431
#)	)\$	2323154315
#	\$	2323154315

## 2.3

$S \rightarrow -S \mid L$

$L \rightarrow a(S) \mid a$

(1)  $S \rightarrow -S$

(2)  $S \rightarrow L$

(3)  $L \rightarrow aL'$

(4)  $L' \rightarrow (S)$

(5)  $L' \rightarrow \epsilon$

	<i>FIRST</i>	<i>FOLLOW</i>
S	-, a	\$, )

	<i>FIRST</i>	<i>FOLLOW</i>
L	a	\$, )
L'	(, ε	\$, )

	<i>a</i>	<i>(</i>	<i>)</i>	<i>-</i>	<i>\$</i>
<i>S</i>	S → L (2)			S → -S (1)	
<i>L</i>	L → aL' (3)				
<i>L'</i>		L' → (S) (4)	L' → ε (5)		L' → ε (5)

#S	-a(-a)\$	ε
#S-	-a(-a)\$	1
#S	a(-a)\$	1
#L	a(-a)\$	12
#L'a	a(-a)\$	123
#L'	(-a)\$	123
#)S(	(-a)\$	1234
#)S	-a)\$	1234
#)S-	-a)\$	12341
#)S	a)\$	12341
#)L	a)\$	123412
#)L'a	a)\$	1234123
#)L'	)\$	1234123
#)	)\$	12341235
#	\$	12341235

## 2.4

$S \rightarrow S^* \mid L$

$L \rightarrow a(S) \mid a$

- (1)  $S \rightarrow LS'$
- (2)  $S' \rightarrow *S'$
- (3)  $S' \rightarrow \epsilon$
- (4)  $L \rightarrow aL'$
- (5)  $L' \rightarrow (S)$
- (6)  $L' \rightarrow \epsilon$

	<i>FIRST</i>	<i>FOLLOW</i>
S	a	\$, )
S'	*, $\epsilon$	\$, )
L	a	*, \$, )
L'	(, $\epsilon$	*, \$, )

	<i>a</i>	<i>(</i>	<i>)</i>	<i>*</i>	<i>\$</i>
<i>S</i>	$S \rightarrow LS'$ (1)				
<i>S'</i>			$S' \rightarrow \epsilon$ (3)	$S' \rightarrow *S'$ (2)	$S' \rightarrow \epsilon$ (3)
<i>L</i>	$L \rightarrow aL'$ (4)				
<i>L'</i>		$L' \rightarrow (S)$ (5)	$L' \rightarrow \epsilon$ (6)	$L' \rightarrow \epsilon$ (6)	$L' \rightarrow \epsilon$ (6)

#S	$a(a^*)*\$$	$\epsilon$
#S'L	$a(a^*)*\$$	1
#S'L'a	$a(a^*)*\$$	14
#S'L'	$(a^*)*\$$	14
#S')S(	$(a^*)*\$$	145
#S')S	$a^*)*\$$	145
#S')S'L	$a^*)*\$$	1451
#S')S'L'a	$a^*)*\$$	14514

#S')S'L'	*)*\$	14514
#S')S'	*)*\$	145146
#S')S'*	*)*\$	1451462
#S')S'	)*\$	1451462
#S')	)*\$	14514623
#S'	*\$	14514623
#S'*	*\$	145146232
#S'	\$	145146232
#	\$	1451462323

## 2.5

$S \rightarrow (S) \mid L$

$L \rightarrow a(S) \mid a$

(1)  $S \rightarrow (S)$

(2)  $S \rightarrow L$

(3)  $L \rightarrow aL'$

(4)  $L' \rightarrow (S)$

(5)  $L' \rightarrow \epsilon$

	<i>FIRST</i>	<i>FOLLOW</i>
S	(, a	\$, )
L	a	\$, )
L'	(, $\epsilon$	\$, )

	<i>a</i>	(	)	\$
<i>S</i>	$S \rightarrow L$ (2)	$S \rightarrow (S)$ (1)		
<i>L</i>	$L \rightarrow aL'$ (3)			

	$a$	$($	$)$	$\$$
$L'$		$L' \rightarrow (S)$ (4)	$L' \rightarrow \epsilon$ (5)	$L' \rightarrow \epsilon$ (5)

#S	(a(a)\$	$\epsilon$
#)S(	(a(a)\$	1
#)S	a(a)\$	1
#)L	a(a)\$	12
#)L'a	a(a)\$	123
#)L'	(a)\$	123
#))S(	(a)\$	1234
#))S	a)\$	1234
#))L	a)\$	12342
#))L'a	a)\$	123423
#))L'	)\$	123423
#))	)\$	1234235
#)	\$	1234235

słowo wejściowe jest niepoprawne, brakuje na końcu ')'

## 2.6

$$E \rightarrow E+V \mid V$$

$$V \rightarrow V*F \mid F$$

$$F \rightarrow a \mid a(E) \mid (E) \mid F^{\wedge}$$

$$(1) \quad E \rightarrow VE'$$

$$(2) \quad E' \rightarrow +VE'$$

$$(3) \quad E' \rightarrow \epsilon$$

$$(4) \quad V \rightarrow FV'$$

$$(5) \quad V' \rightarrow *FV'$$

$$(6) \quad V' \rightarrow \epsilon$$

$$(7) \quad F \rightarrow (E)F'$$

(8)  $F \rightarrow aF''$

(9)  $F'' \rightarrow F'$

(A)  $F'' \rightarrow (E)F'$

(B)  $F' \rightarrow \wedge F'$

(C)  $F' \rightarrow \varepsilon$

	<i>FIRST</i>	<i>FOLLOW</i>
E	(, a	\$, )
E'	+, $\varepsilon$	\$, )
V	(, a	+, \$, )
V'	*, $\varepsilon$	+, \$, )
F	(, a	*, +, \$, )
F'	$\wedge$ , $\varepsilon$	*, +, \$, )
F''	(, $\wedge$ , $\varepsilon$	*, +, \$, )

	<i>a</i>	(	)	+	*	$\wedge$	\$
<b>E</b>	$E \rightarrow VE'$ (1)	$E \rightarrow VE'$ (1)					
<b>E'</b>			$E' \rightarrow \varepsilon$ (3)	$E' \rightarrow +VE'$ (2)			$E' \rightarrow \varepsilon$ (3)
<b>V</b>	$V \rightarrow FV'$ (4)	$V \rightarrow FV'$ (4)					
<b>V'</b>			$V' \rightarrow \varepsilon$ (6)	$V' \rightarrow \varepsilon$ (6)	$V' \rightarrow *FV'$ (5)		$V' \rightarrow \varepsilon$ (6)
<b>F</b>	$F \rightarrow aF''$ (8)	$F \rightarrow (E)F'$ (7)					
<b>F'</b>			$F' \rightarrow \varepsilon$ (C)	$F' \rightarrow \varepsilon$ (C)	$F' \rightarrow \varepsilon$ (C)	$F' \rightarrow \wedge F'$ (B)	$F' \rightarrow \varepsilon$ (C)
<b>F''</b>		$F'' \rightarrow (E)F'$ (A)	$F'' \rightarrow F'$ (9)	$F'' \rightarrow F'$ (9)	$F'' \rightarrow F'$ (9)	$F'' \rightarrow F'$ (9)	$F'' \rightarrow F'$ (9)

#E	$(a+a(a^\wedge)*a)+a\$ \ \varepsilon$
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#E'V	$(a+a(a^)*a)+a\$$	1
#E'V'F	$(a+a(a^)*a)+a\$$	14
#E'V'F')E(	$(a+a(a^)*a)+a\$$	147
#E'V'F')E	$a+a(a^)*a)+a\$$	147
#E'V'F')E'V	$a+a(a^)*a)+a\$$	1471
#E'V'F')E'V'F	$a+a(a^)*a)+a\$$	14714
#E'V'F')E'V'F"a	$a+a(a^)*a)+a\$$	147148
#E'V'F')E'V'F"	$+a(a^)*a)+a\$$	147148
#E'V'F')E'V'F'	$+a(a^)*a)+a\$$	1471489
#E'V'F')E'V'	$+a(a^)*a)+a\$$	1471489C
#E'V'F')E'	$+a(a^)*a)+a\$$	1471489C6
#E'V'F')E'V+	$+a(a^)*a)+a\$$	1471489C62
#E'V'F')E'V	$a(a^)*a)+a\$$	1471489C62
#E'V'F')E'V'F	$a(a^)*a)+a\$$	1471489C624
#E'V'F')E'V'F"a	$a(a^)*a)+a\$$	1471489C6248
#E'V'F')E'V'F"	$(a^)*a)+a\$$	1471489C6248
#E'V'F')E'V'F')E(	$(a^)*a)+a\$$	1471489C6248A
#E'V'F')E'V'F')E	$a^)*a)+a\$$	1471489C6248A
#E'V'F')E'V'F')E'V	$a^)*a)+a\$$	1471489C6248A1
#E'V'F')E'V'F')E'V'F	$a^)*a)+a\$$	1471489C6248A14
#E'V'F')E'V'F')E'V'F"a	$a^)*a)+a\$$	1471489C6248A148
#E'V'F')E'V'F')E'V'F"	$^)*a)+a\$$	1471489C6248A148
#E'V'F')E'V'F')E'V'F'	$^)*a)+a\$$	1471489C6248A1489
#E'V'F')E'V'F')E'V'F'^	$^)*a)+a\$$	1471489C6248A1489B
#E'V'F')E'V'F')E'V'F'	$)*a)+a\$$	1471489C6248A1489B
#E'V'F')E'V'F')E'V'	$)*a)+a\$$	1471489C6248A1489BC
#E'V'F')E'V'F')E'	$)*a)+a\$$	1471489C6248A1489BC6
#E'V'F')E'V'F')	$)*a)+a\$$	1471489C6248A1489BC63
#E'V'F')E'V'F'	$*a)+a\$$	1471489C6248A1489BC63

#E'V'F')E'V'	*a)+a\$	1471489C6248A1489BC63C
#E'V'F')E'V'F*	*a)+a\$	1471489C6248A1489BC63C5
#E'V'F')E'V'F	a)+a\$	1471489C6248A1489BC63C5
#E'V'F')E'V'F"a	a)+a\$	1471489C6248A1489BC63C58
#E'V'F')E'V'F"	)a+\$	1471489C6248A1489BC63C58
#E'V'F')E'V'F'	)a+\$	1471489C6248A1489BC63C589
#E'V'F')E'V'	)a+\$	1471489C6248A1489BC63C589C
#E'V'F')E'	)a+\$	1471489C6248A1489BC63C589C6
#E'V'F')	)a+\$	1471489C6248A1489BC63C589C63
#E'V'F'	+a\$	1471489C6248A1489BC63C589C63
#E'V'	+a\$	1471489C6248A1489BC63C589C63C
#E'	+a\$	1471489C6248A1489BC63C589C63C6
#E'V+	+a\$	1471489C6248A1489BC63C589C63C62
#E'V	a\$	1471489C6248A1489BC63C589C63C62
#E'V'F	a\$	1471489C6248A1489BC63C589C63C624
#E'V'F"a	a\$	1471489C6248A1489BC63C589C63C6248
#E'V'F"	\$	1471489C6248A1489BC63C589C63C6248
#E'V'F'	\$	1471489C6248A1489BC63C589C63C62489
#E'V'	\$	1471489C6248A1489BC63C589C63C62489C
#E'	\$	1471489C6248A1489BC63C589C63C62489C6
#	\$	1471489C6248A1489BC63C589C63C62489C63

## 2.7

$E \rightarrow E+V \mid V$

$V \rightarrow -V \mid F$

$F \rightarrow a \mid a(E) \mid (E) \mid F^*$

(1)  $E \rightarrow VE'$

(2)  $E' \rightarrow +VE'$

(3)  $E' \rightarrow \varepsilon$

- (4)  $V \rightarrow -V$
- (5)  $V \rightarrow F$
- (6)  $F' \rightarrow (E)$
- (7)  $F' \rightarrow \epsilon$
- (8)  $F \rightarrow aF'F''$
- (9)  $F \rightarrow (E)F''$
- (A)  $F'' \rightarrow *F''$
- (B)  $F' \rightarrow \epsilon$

	<i>FIRST</i>	<i>FOLLOW</i>
E	(, a, -	\$, )
E'	$\epsilon$ , +	\$, )
V	(, a, -	+, \$, )
F	(, a	+, \$, )
F'	$\epsilon$ , (	*, +, \$, )
F''	$\epsilon$ , *	+, \$, )

	<i>a</i>	(	)	-	+	*	\$
<i>E</i>	$E \rightarrow VE'$ (1)	$E \rightarrow VE'$ (1)		$E \rightarrow VE'$ (1)			
<i>E'</i>			$E' \rightarrow \epsilon$ (3)		$E' \rightarrow +VE'$ (2)		$E' \rightarrow \epsilon$ (3)
<i>V</i>	$V \rightarrow F$ (5)	$V \rightarrow F$ (5)		$V \rightarrow -V$ (4)			
<i>F</i>	$F \rightarrow aF'F''$ (8)	$F \rightarrow (E)F''$ (9)					
<i>F'</i>		$F' \rightarrow (E)$ (6)	$F' \rightarrow \epsilon$ (7)		$F' \rightarrow \epsilon$ (7)	$F' \rightarrow \epsilon$ (7)	$F' \rightarrow \epsilon$ (7)
<i>F''</i>			$F' \rightarrow \epsilon$ (B)		$F' \rightarrow \epsilon$ (B)	$F'' \rightarrow *F''$ (A)	$F' \rightarrow \epsilon$ (B)

#E	$(-a+a(a^*)) + a\$$	$\epsilon$
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#E'V	$(-a+a(a^*))+a\$$	1
#E'F	$(-a+a(a^*))+a\$$	15
#E'F'')E(	$(-a+a(a^*))+a\$$	159
#E'F'')E	$-a+a(a^*))+a\$$	159
#E'F'')E'V	$-a+a(a^*))+a\$$	1591
#E'F'')E'V-	$-a+a(a^*))+a\$$	15914
#E'F'')E'V	$a+a(a^*))+a\$$	15914
#E'F'')E'F	$a+a(a^*))+a\$$	159145
#E'F'')E'F'F'a	$a+a(a^*))+a\$$	1591458
#E'F'')E'F'F'	$+a(a^*))+a\$$	1591458
#E'F'')E'F''	$+a(a^*))+a\$$	15914587
#E'F'')E'	$+a(a^*))+a\$$	15914587B
#E'F'')E'V+	$+a(a^*))+a\$$	15914587B2
#E'F'')E'V	$a(a^*))+a\$$	15914587B2
#E'F'')E'F	$a(a^*))+a\$$	15914587B25
#E'F'')E'F'F'a	$a(a^*))+a\$$	15914587B258
#E'F'')E'F'F'	$(a^*))+a\$$	15914587B258
#E'F'')E'F'')E(	$(a^*))+a\$$	15914587B2586
#E'F'')E'F'')E	$a^*))+a\$$	15914587B2586
#E'F'')E'F'')E'V	$a^*))+a\$$	15914587B25861
#E'F'')E'F'')E'F	$a^*))+a\$$	15914587B258615
#E'F'')E'F'')E'F'F'a	$a^*))+a\$$	15914587B2586158
#E'F'')E'F'')E'F'F'	$^*))+a\$$	15914587B2586158
#E'F'')E'F'')E'F''	$^*))+a\$$	15914587B25861587
#E'F'')E'F'')E'F''*	$^*))+a\$$	15914587B25861587A
#E'F'')E'F'')E'F''	$))+a\$$	15914587B25861587A
#E'F'')E'F'')E'	$))+a\$$	15914587B25861587AB
#E'F'')E'F'')E'F'')	$))+a\$$	15914587B25861587AB3
#E'F'')E'F'')	$))+a\$$	15914587B25861587AB3

#E'F'')E'	) + a \$	15914587B25861587AB3B
#E'F')	) + a \$	15914587B25861587AB3B3
#E'F''	+ a \$	15914587B25861587AB3B3
#E'	+ a \$	15914587B25861587AB3B3B
#E'V+	+ a \$	15914587B25861587AB3B3B2
#E'V	a \$	15914587B25861587AB3B3B2
#E'F	a \$	15914587B25861587AB3B3B25
#E'F''F'a	a \$	15914587B25861587AB3B3B258
#E'F''F'	\$	15914587B25861587AB3B3B258
#E'F''	\$	15914587B25861587AB3B3B2587
#E'	\$	15914587B25861587AB3B3B2587B
#	\$	15914587B25861587AB3B3B2587B3

## 2.8

$S \rightarrow L=E$

$L \rightarrow a \mid a(E)$

$E \rightarrow E+V \mid V$

$V \rightarrow a \mid a(E) \mid (E)$

(1)  $S \rightarrow L=E$

(2)  $L \rightarrow aL'$

(3)  $L' \rightarrow \varepsilon$

(4)  $L' \rightarrow (E)$

(5)  $E \rightarrow VE'$

(6)  $E' \rightarrow +VE'$

(7)  $E' \rightarrow \varepsilon$

(8)  $V \rightarrow (E)$

(9)  $V \rightarrow aV'$

(A)  $V' \rightarrow \varepsilon$

(B)  $V' \rightarrow (E)$

	<i>FIRST</i>	<i>FOLLOW</i>
S	a	\$,
L	a	=
L'	(, ε	=
E	a, (	), \$
E'	ε, +	), \$
V	a, (	+, ), \$
V'	(, ε	+, ), \$

	<i>a</i>	<i>(</i>	<i>)</i>	<i>+</i>	<i>=</i>	<i>\$</i>
<i>S</i>	$S \rightarrow L=E$ (1)					
<i>L</i>	$L \rightarrow aL'$ (2)					
<i>L'</i>		$L' \rightarrow (E)$ (4)			$L' \rightarrow \epsilon$ (3)	
<i>E</i>	$E \rightarrow VE'$ (5)	$E \rightarrow VE'$ (5)				
<i>E'</i>			$E' \rightarrow \epsilon$ (7)	$E' \rightarrow +VE'$ (6)		$E' \rightarrow \epsilon$ (7)
<i>V</i>	$V \rightarrow aV'$ (9)	$V \rightarrow (E)$ (8)				
<i>V'</i>		$V' \rightarrow (E)$ (B)	$V' \rightarrow \epsilon$ (A)	$V' \rightarrow \epsilon$ (A)		$V' \rightarrow \epsilon$ (A)

#S	$a(a+a)=a+a(a)\$$	ε
#E=L	$a(a+a)=a+a(a)\$$	1
#E=L'a	$a(a+a)=a+a(a)\$$	12
#E=L'	$(a+a)=a+a(a)\$$	12
#E=)E(	$(a+a)=a+a(a)\$$	124
#E=)E	$a+a)=a+a(a)\$$	124
#E=)E'V	$a+a)=a+a(a)\$$	1245

#E=)E'V'a	a+a)=a+a(a)\$	12459
#E=)E'V'	+a)=a+a(a)\$	12459
#E=)E'	+a)=a+a(a)\$	12459A
#E=)E'V+	+a)=a+a(a)\$	12459A6
#E=)E'V	a)=a+a(a)\$	12459A6
#E=)E'V'a	a)=a+a(a)\$	12459A69
#E=)E'V'	)=a+a(a)\$	12459A69
#E=)E'V'	)=a+a(a)\$	12459A69
#E=)E'	)=a+a(a)\$	12459A69A
#E=)	)=a+a(a)\$	12459A69A7
#E=	=a+a(a)\$	12459A69A7
#E	a+a(a)\$	12459A69A7
#E'V	a+a(a)\$	12459A69A75
#E'V'a	a+a(a)\$	12459A69A759
#E'V'	+a(a)\$	12459A69A759
#E'	+a(a)\$	12459A69A759A
#E'V+	+a(a)\$	12459A69A759A6
#E'V	a(a)\$	12459A69A759A6
#E'V'a	a(a)\$	12459A69A759A69
#E'V'	(a)\$	12459A69A759A69
#E')E(	(a)\$	12459A69A759A69B
#E')E	a)\$	12459A69A759A69B
#E')E'V	a)\$	12459A69A759A69B5
#E')E'V'a	a)\$	12459A69A759A69B59
#E')E'V'	)\$	12459A69A759A69B59
#E')E'	)\$	12459A69A759A69B59A
#E')	)\$	12459A69A759A69B59A7
#E'	\$	12459A69A759A69B59A7
#	\$	12459A69A759A69B59A77